

MODELING HEAT PRODUCTION BY AOX PATHWAY IN SINGLE CELL

Assumptions

1. The non-growth rate of ATP production is 7.6 mmol per gram of biomass per hour (E. coli W3110) at 38C. This rate is slightly higher in growth-associated conditions (13 mmol/g/h). (Varma & Palsson, 1994)
2. AOX branches from the cytochrome pathway at the level of the ubiquinone pool and couples the oxidation of ubiquinol to the four-electron reduction of oxygen to water. (Albury, Elliott & Moore, 2009)
3. Electrochemical potential gradient difference between Uq and O₂ is 800 mV (Ingledeew & Poole, 1984)
4. Two electrons are required per production of 1 ATP molecule
5. The dry mass of one E. coli cell = 7×10^{-13} g (<http://bionumbers.hms.harvard.edu/bionumber.aspx?s=y&id=103904&ver=9>)

Calculations

The amount of energy released by 4 electrons is given by:

$$\begin{aligned} \text{V o l t} &= \frac{\text{J o u l e}}{\text{C o u l o m b}} \Rightarrow \\ 800 \times 10^{-3} &= \frac{\text{J o u l e s}}{(4 \text{ e l e c t r o n s})(1.6 \times 10^{-19} \text{ C})} \\ \text{E n e r g y r e l e a s e d} &= 5.12 \times 10^{-19} \text{ J o u l e s} \end{aligned}$$

The amount of energy per cell per second is given by:

$$\begin{aligned} &\frac{7.6 \times 10^{-3} \text{ m o l A T P}}{3600 \text{ s e c} \times \text{g. b i o m a s s}} \times \frac{2 \text{ m o l e l e c}}{\text{m o l e A T P}} \times \frac{6.0223 \times 10^{23} \text{ e l e c t r o n s}}{\text{m o l e l e c}} \times \left(\frac{5.12 \times 10^{-19} \text{ J}}{4 \text{ e l e c t r o n s}} \right) \times 0.7 \\ &= 0.2278 \frac{\text{J}}{\text{g b i o m a s s} \times \text{s e c}} = 1.6 \times 10^{-13} \frac{\text{J}}{\text{c e l l} \times \text{s e c}} \end{aligned}$$

(where 0.7 is an efficiency factor representing approximately 70% conversion of electrons in the pathway in sacred lotus cells [Applied and Environmental Microbiology, Oct. 1994, p. 3724-3731 Vol 60 No 10])

By way of comparison, the specific heat of water is 4.187 J per ml (when 1 ml = 1 gram).

Characterization methods

There are currently a few possible ways to characterize the heat production that largely break down into two categories: measuring in saturated bulk solution, and measuring colonies on a plate.

Measuring in saturated bulk solution:

Measuring in bulk means heating up solution and measuring either with sensitive thermometers or isothermal calorimetry. Taking a saturated 1 ml sample in solution would take an inordinate amount of time to see even a 1 C rise:

$$1 \text{ ml} \times 1 \times 10^{10} \frac{\text{cells}}{\text{ml}} \times 1.6 \times 10^{-13} \frac{\text{J}}{\text{cell} \times \text{sec}} = 1.6 \times 10^{-4} \frac{\text{J}}{\text{sec}}$$
$$4.187 \frac{\text{J}}{\text{ml}} \times \frac{\text{seconds}}{1.6 \times 10^{-4} \text{ J}} = 2,417 \text{ seconds} \times \frac{1 \text{ min}}{60 \text{ sec}} = 40.3 \text{ minutes}$$

Methods such as isothermal calorimetry have very precise detection ranges on the order of several microcal/sec that could possibly determine a temperature shift that happens in the timeframe of minutes instead of hours.

Measuring in colonies:

There are several types of thermal imaging that could possibly detect heat from colonies on a plate with a precision of approximately 0.1 C.